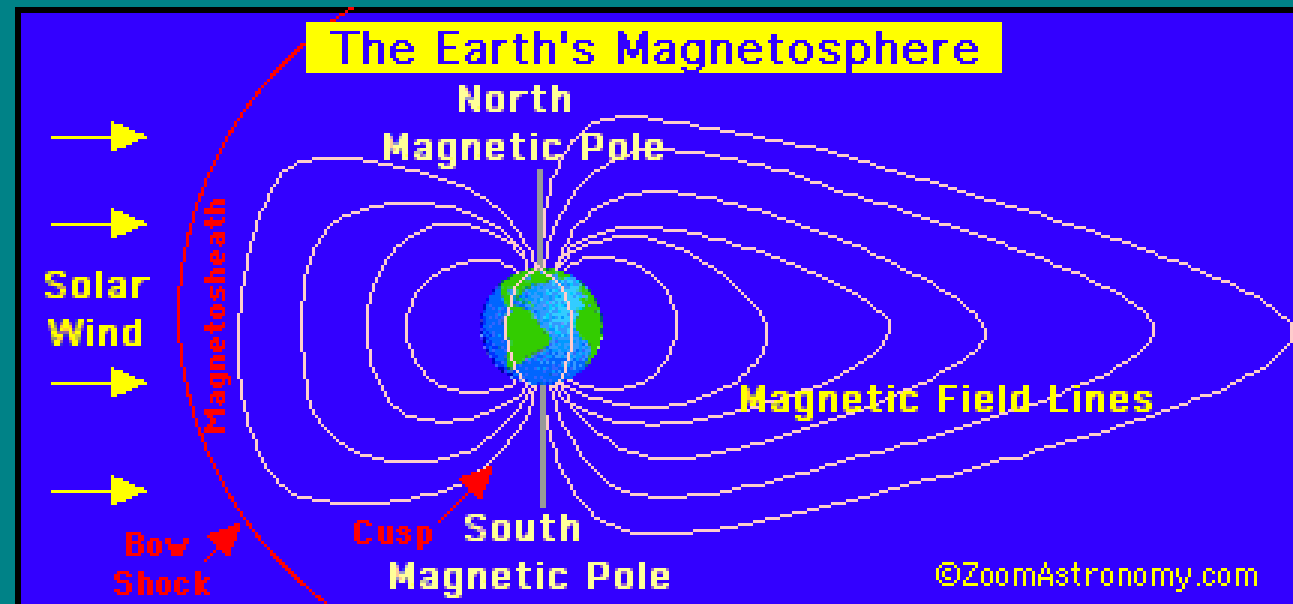


05_Electromagnetic principles

Electromagnetic principles

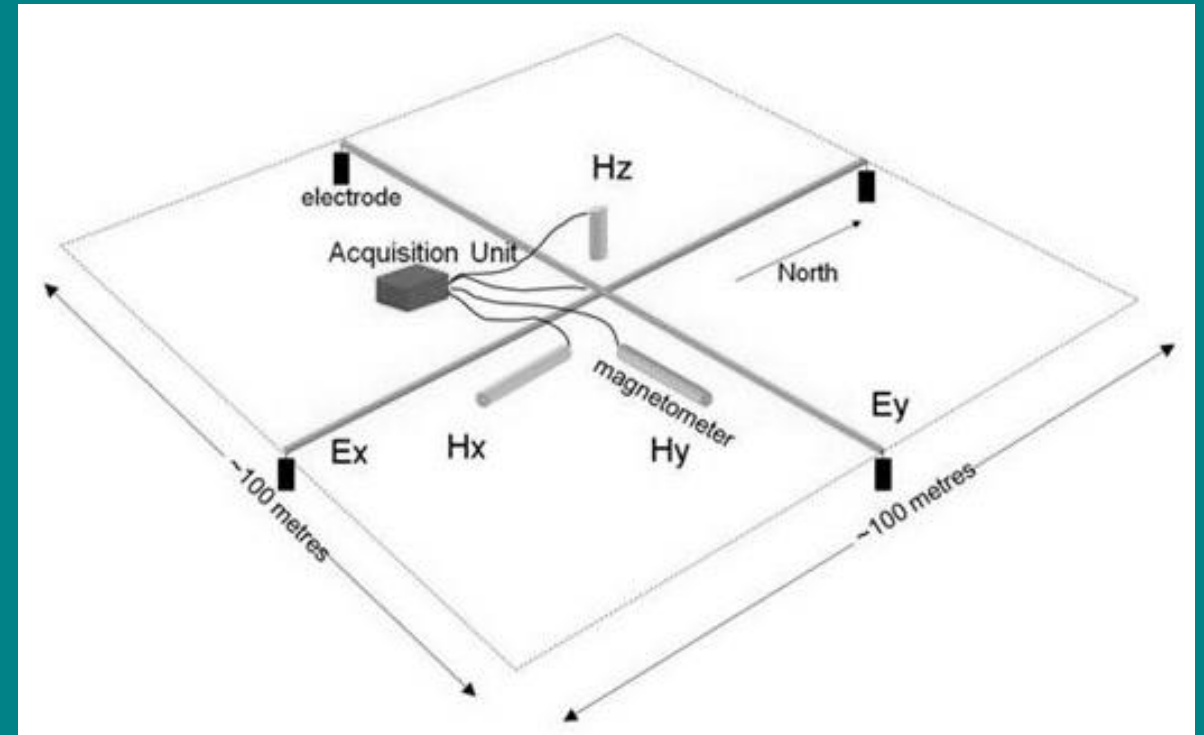
- During a MT experiment, we measure the **time-variations** in the **electromagnetic field** of the Earth
- Caused by magnetic storms (freq. < 1 Hz) and lightning activity (freq. > 1 Hz).



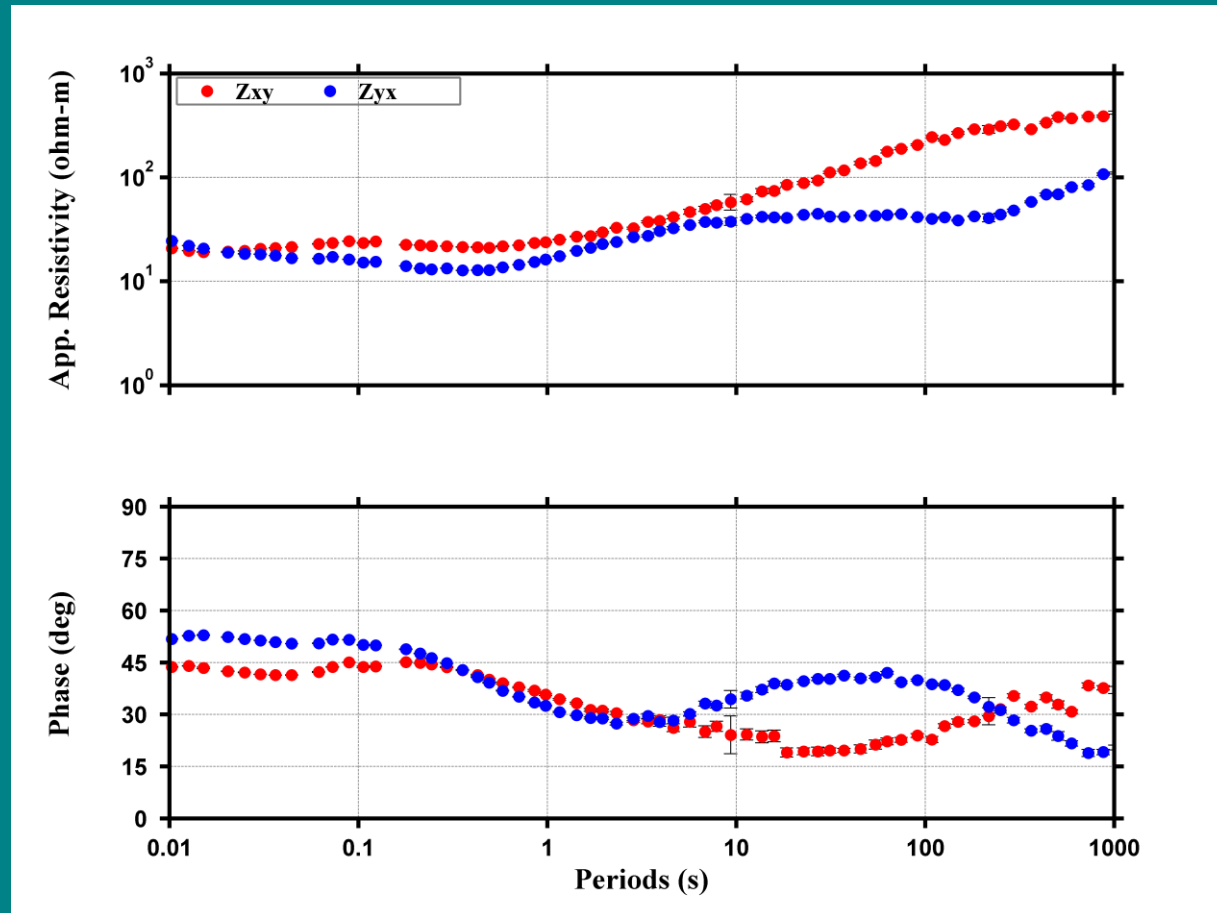
Magnetotelluric measurement

Measures the time-variations in the horizontal electric fields (E_x and E_y) as well as the the horizontal and vertical magnetic fields (B_x , B_y and B_z).

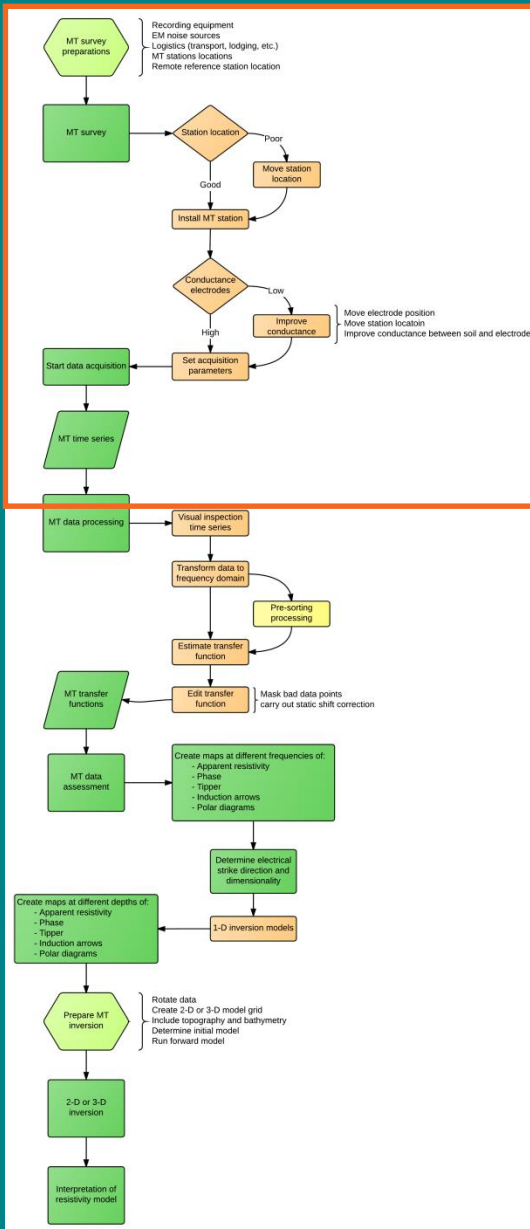
- E-fields are measured with (polarized) electrodes.
- B-fields are measured with magnetic coils.
- The 5 fields are recorded (in time) by a car battery powered data-logger.



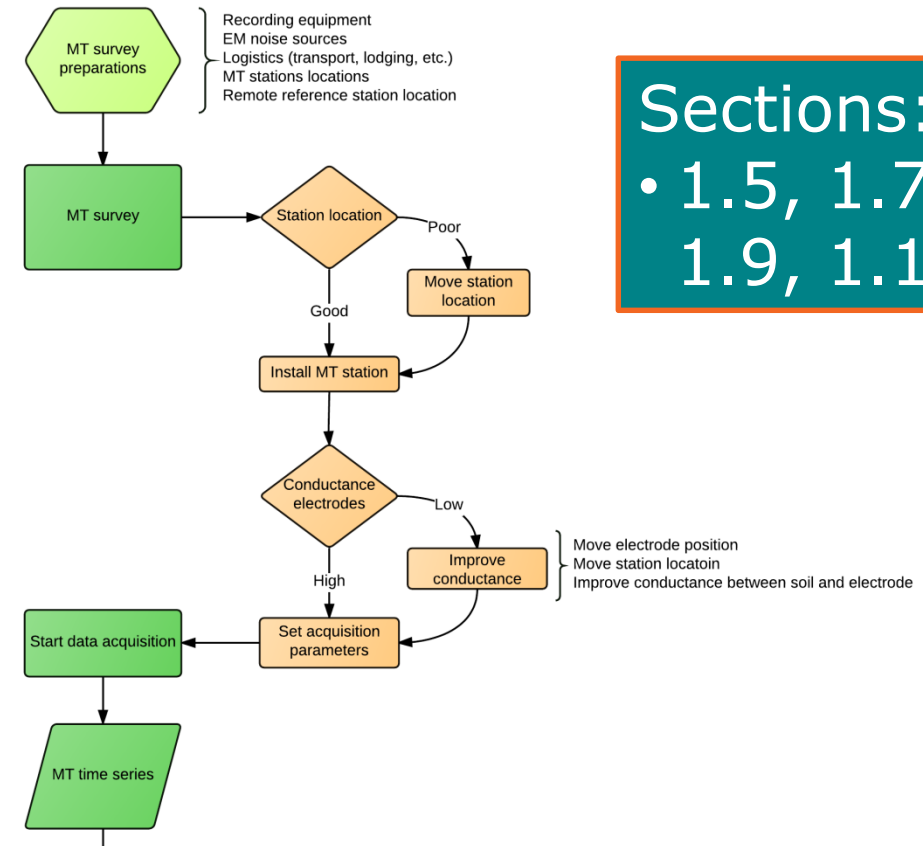
Magnetotelluric response



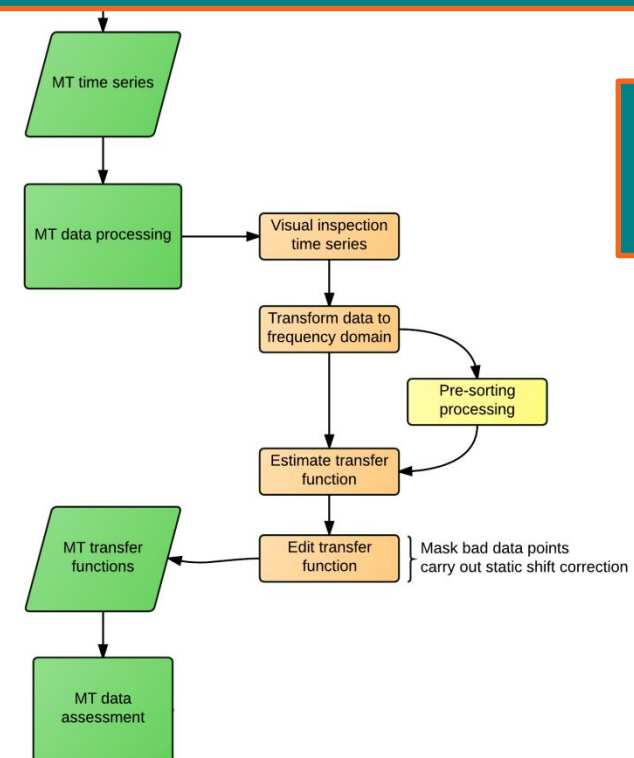
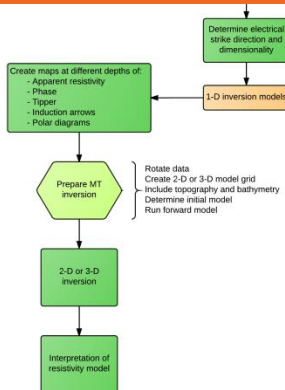
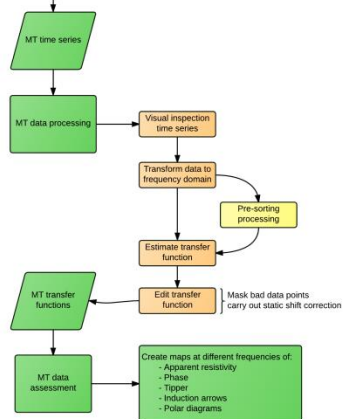
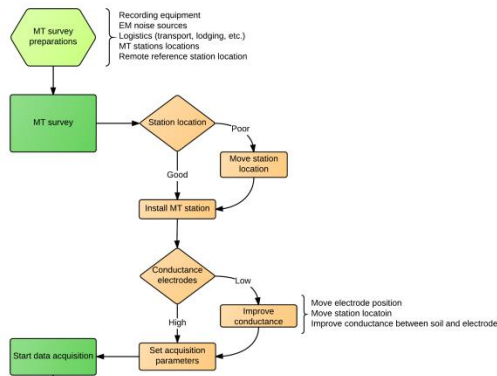
The MT process (1)



Sections:
• 1.5, 1.7, 1.8,
1.9, 1.10, 1.11

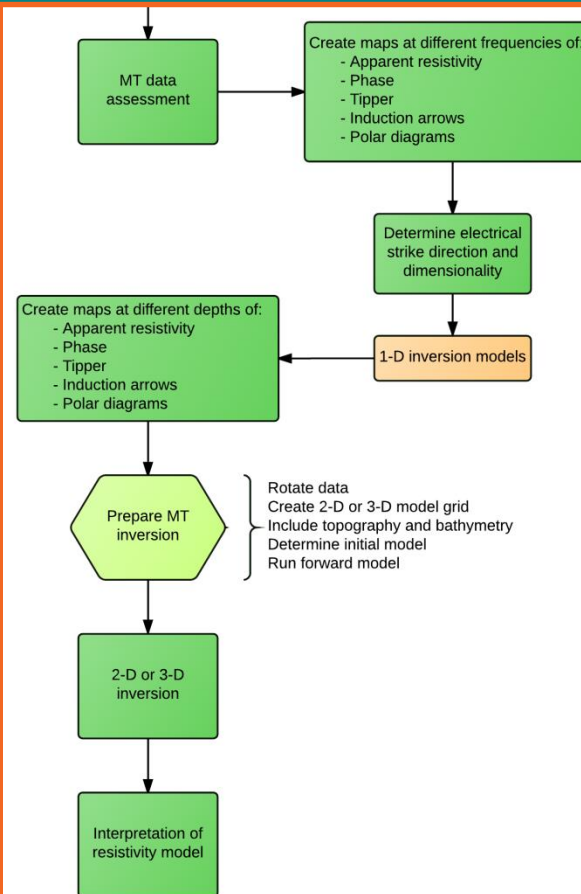
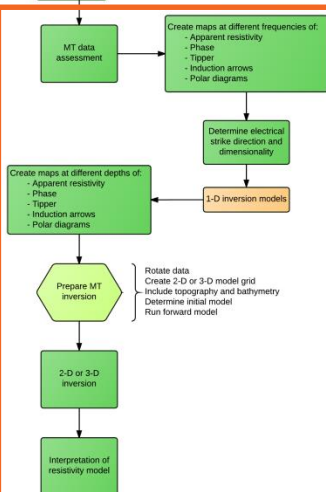
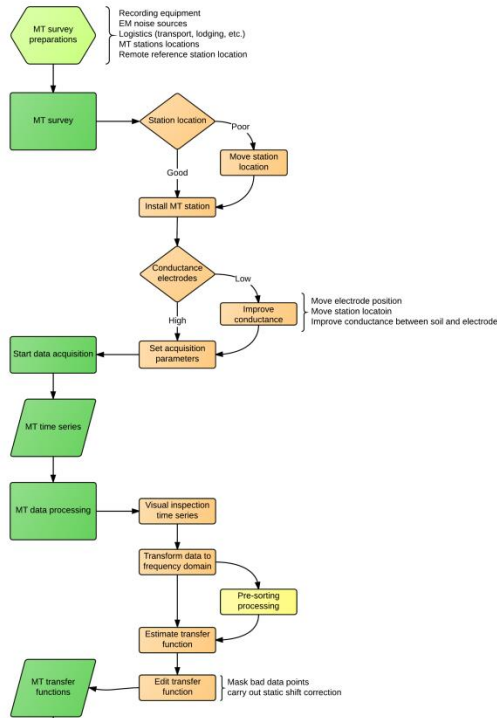


The MT process (2)



Sections:
• 1.5, 1.6, 1.11

The MT process (3)



Sections:

1.2, 1.3, 1.4
1.5, 1.6, 1.12,
1.13

Very short history of electromagnetics

- Electric response of the *deep* Earth retrieved by measuring *longer* (Rikitake, 1948; Tikhonov, 1950; Cagnaird, 1953).
 - **Magnetotellurics (MT)**; low frequency (0.001 Hz – 300 Hz).
 - **Audio-magnetotellurics (AMT)**; mid frequency (10 Hz – 10 kHz), 1960's.
 - **Controlled-source audio-magnetotellurics (CSAMT)**; high frequency (1 Hz – 2 kHz), 1970's (e.g. Goldstein; 1971, Strangway; 1975), Zonge; 1980).

Electromagnetic methods

no.	EM method	Signal source		Frequency	Depth	Application
1	MT	Solar wind Lightning	➤ Passive	Low	100 m – 100 km	Geothermal Hydrocarbon Mineral Crust and mantle studies
2	AMT		➤ Active	Mid	< 3 km	Geothermal Mineral
3	CSAMT/CSEM	Grounded dipole	➤ Active	High	< 3 km	Geothermal Hydrocarbon Mineral
4	TDEM ¹	Transmitting loop	➤ Active	High	< 500 m	MT static shift correction
5	VES, GPR, ...		➤ Active	High	< 500 m	e.g. infrastructure Archeology

¹Time-domain electromagnetics

Electromagnetic skin depth (1)

- **Electromagnetic skin depth relation:**

$$p(T) \approx 500 \sqrt{T \rho_a}$$

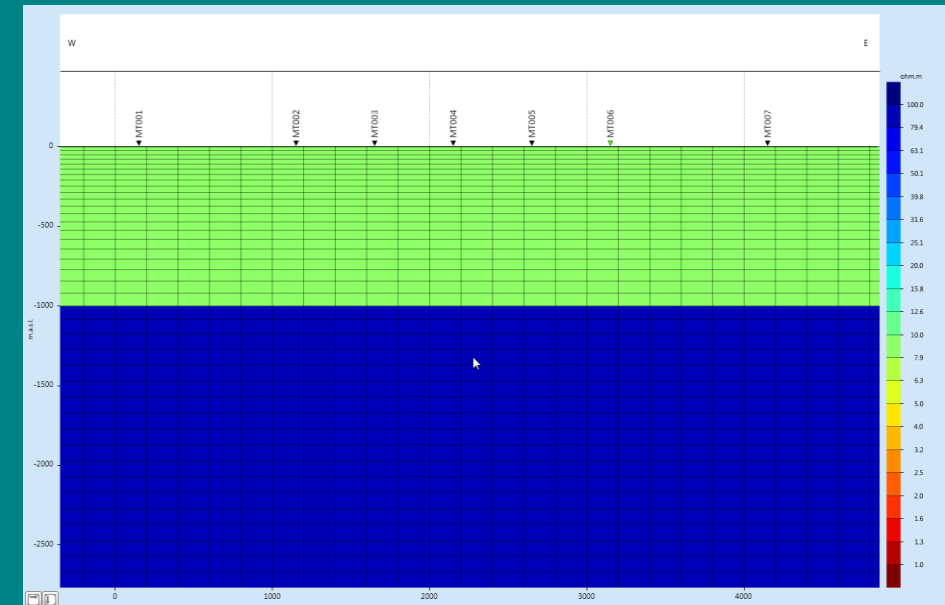
where $p(T)$ is the EM skin depth in metres (m), T is the sounding period in seconds (s), ρ_a is apparent bulk resistivity in Ohm-metre (Ωm).

Electromagnetic skin depth (2)

$$p(T) \approx 500 \sqrt{T \rho_a} \quad \text{or} \quad T = \mu_0 \sigma \pi p^2$$

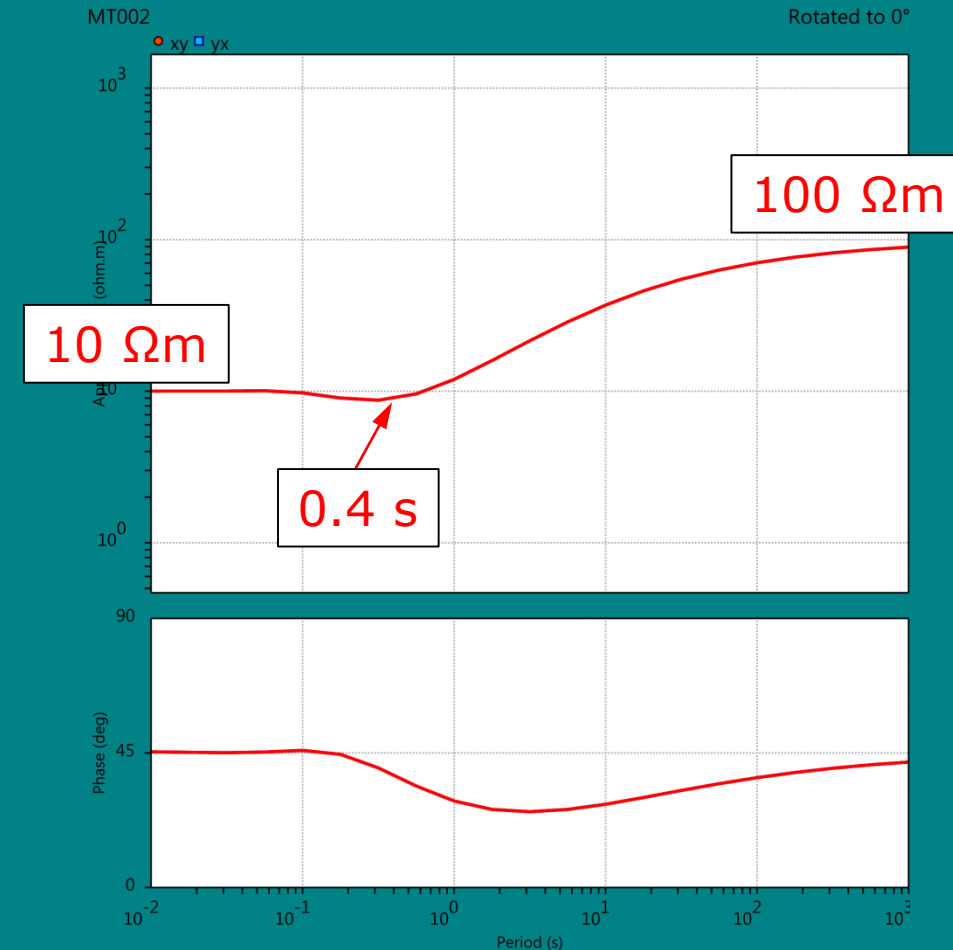
- Consider a layered Earth:

Layer	Thickness	Resistivity
Top layer	1,000 m	10 Ωm
Basement	∞	100 Ωm



Electromagnetic skin depth (3)

- Base of layer visible in apparent resistivity at ~ 0.4 s.
- Bulk electrical resistivity of the Earth ranges from 10^{-1} to 10^5 Ωm .
- Target depths range from 500 m to 100 km
- Frequency range utilized in MT: 10^{-4} to 10^5 s
- For geothermal exploration: 10^{-4} to 1,000 s



Assumptions of the MT method

- Maxwell's equations are obeyed
- The Earth does not generate EM energy
- Normally incident EM waves on the Earth's surface are uniform and planar (**plane-wave assumption**)
- ...
- and more, see e.g. Simpson and Bahr (2005)

Plane wave assumption

- A plane wave propagates normal to a plane in which the fields are constant.
- The *impedance tensor* at a specific location is always the same, independent of when the fields are recorded.
 - Very shallow surface conditions change (geology)

Maxwell equations (1)

- Gauss' law for electric fields:
 - Opposite charges attract and negative charges repel
- Gauss' law for magnetic fields:
 - Magnetic monopoles do not exist
- Faraday's law
- Ampere's law

Maxwell equations (2)

- **Faraday's law:**

- Electric current gives rise to magnetic fields. Magnetic fields around a circuit gives rise to electric current.
- A time-varying magnetic field gives rise to an electric field circulating around it.
- A circulating electric field in time gives rise to a time-varying magnetic field.

Maxwell equations (3)

- **Ampere's law:**

- A flowing electric current gives rise to a magnetic field that circles around it
- A time-varying electric flux density gives rise to a magnetic field that circles around it.

- In combination with Faraday's law:

- A time-varying magnetic field gives rise to a (perpendicular flowing) time-varying electric field. And a time-varying electric field gives rise to a (perpendicular flowing) time-varying magnetic field – which will produce a time-varying (perpendicular flowing) electric field, etc.